



# Sensitivity analysis

Development of crop ideotypes

## Uncertainty in sensitivity analysis

- Sensitivity analysis **methods** have **their own parameters**

e.g., levels and trajectories for Morris, number of executions for all other methods

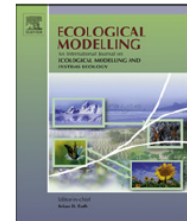
Ecological Modelling 221 (2010) 1897–1906



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journal homepage: [www.elsevier.com/locate/ecolmodel](http://www.elsevier.com/locate/ecolmodel)



Comparison of sensitivity analysis techniques: A case study with the rice model WARM

R. Confalonieri<sup>a,\*</sup>, G. Bellocchi<sup>b</sup>, S. Bregaglio<sup>a,b</sup>, M. Donatelli<sup>b,c</sup>, M. Acutis<sup>a</sup>



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- Sensitivity analysis **methods** have **their own parameters**
  - ✓ **Concordance among rankings** (Top-Down Concordance Coefficient, TDCC):

$$TDCC = \frac{\sum_{i=1}^N [\sum_{j=1}^{nSA} SS(SM_{ij})] - nSA^2 \cdot N}{nSA^2 \cdot \left( N - \sum_{i=1}^N \frac{1}{i} \right)}$$

where

- $nSA$  is the number of sensitivity analysis results to be compared
- $SS(SM_{ij})$  is the Savage Score of  $x_{ij}$



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  - ✓ **Concordance** among rankings is considered **NON significant** for **p-values > 0.05**.
  - ✓ with **p-value** calculated according to the **statistic T**, which **approximates a  $X^2$**  distribution with **N-1 degrees of freedom**:

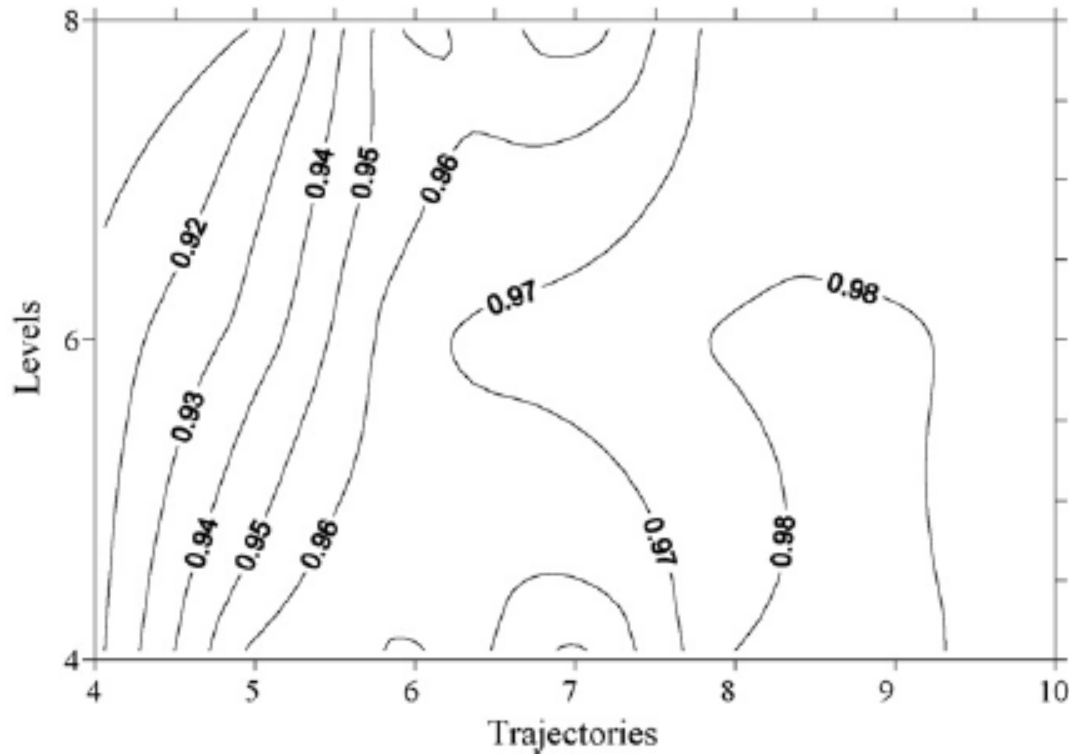
$$T = nSA \cdot (N - 1) \cdot TDCC$$

- ✓ **Null hypothesis** is **absence of concordance**.



## Uncertainty in sensitivity analysis

- Sensitivity analysis **methods** have **their own parameters**



**Fig. 1.** Morris robustness. Top-down concordance coefficient (TDCC) calculated on rankings obtained, for each combination trajectory  $\times$  level, with seven different seeds ( $p$ -values always lower than  $10^{-9}$ ).



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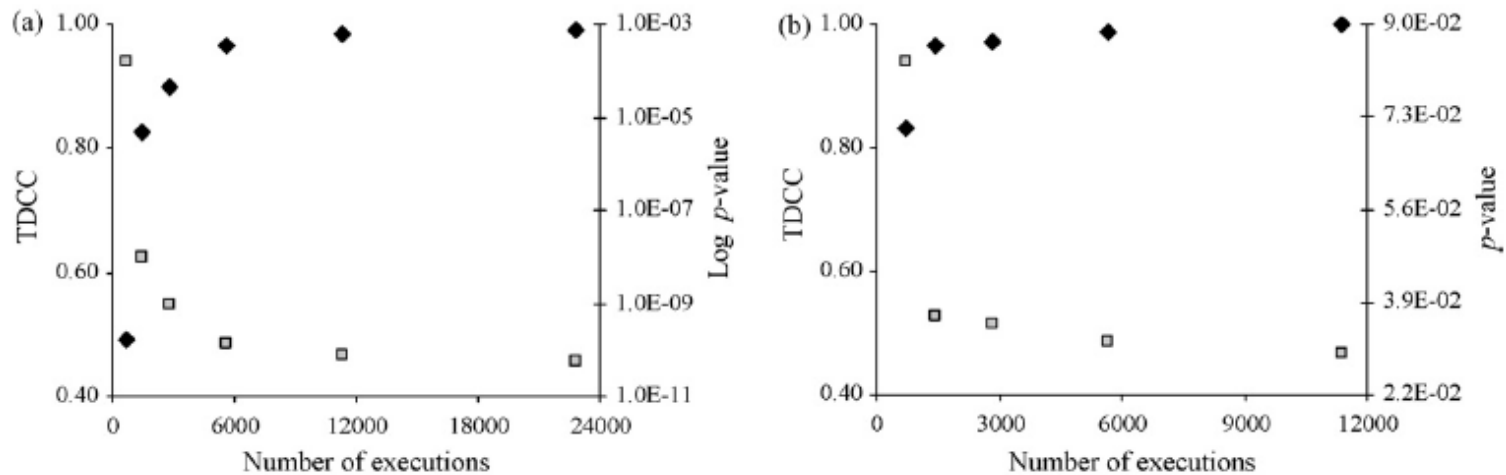


Fig. 5. E-FAST robustness. Top-down concordance coefficient (TDCC; black diamonds) and related  $p$ -values (grey squares) calculated for different method parameterizations. (a) Effect of seven different seeds in influencing parameters ranking for increasing number of model executions. (b) Comparison between the ranking obtained with 22,803 model executions and those obtained increasing the number of executions.

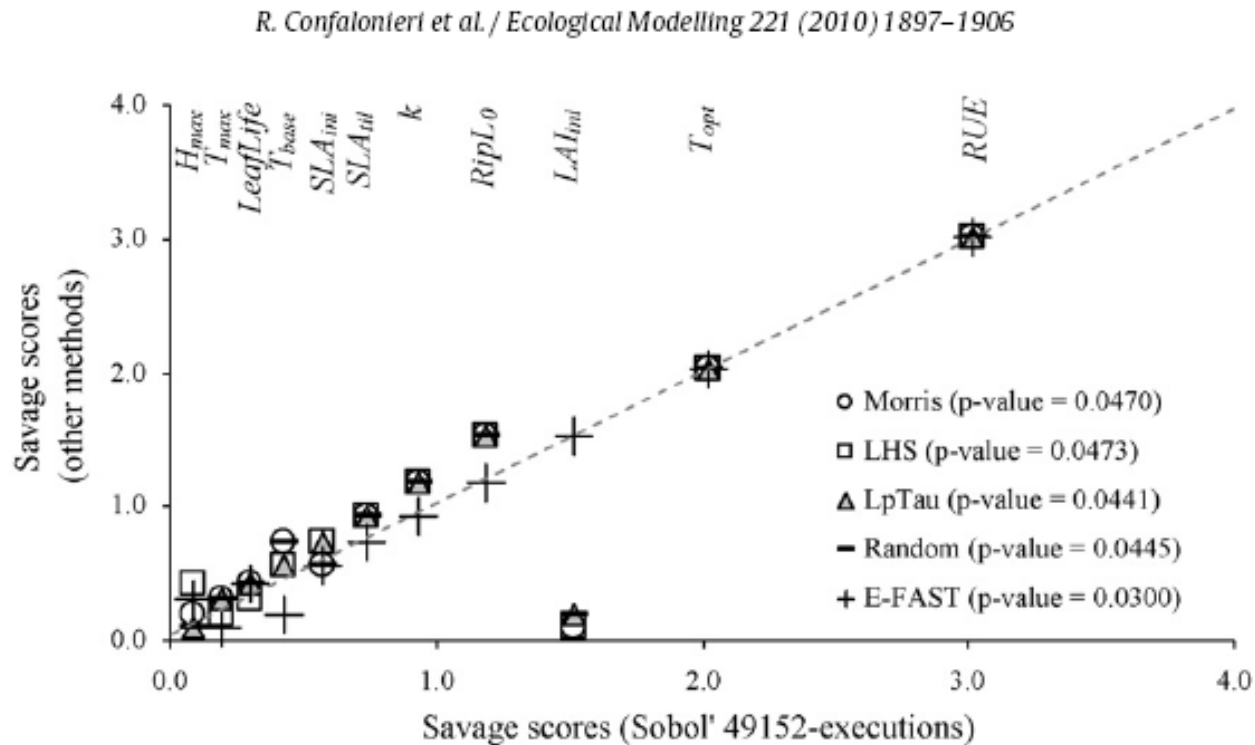


# Sensitivity analysis

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## Uncertainty in sensitivity analysis

- Sensitivity analysis **methods** have **their own parameters**





# Sensitivity analysis

Development of crop ideotypes

## Uncertainty in sensitivity analysis

- Most **methods** are very sensitive to **parameter distributions**

Ecological Modelling 340 (2016) 57–63

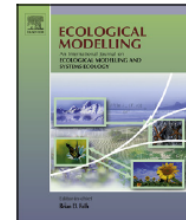


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Sensitivity analysis of a sensitivity analysis: We are likely overlooking the impact of distributional assumptions

Livia Paleari<sup>a</sup>, Roberto Confalonieri<sup>b,\*</sup>



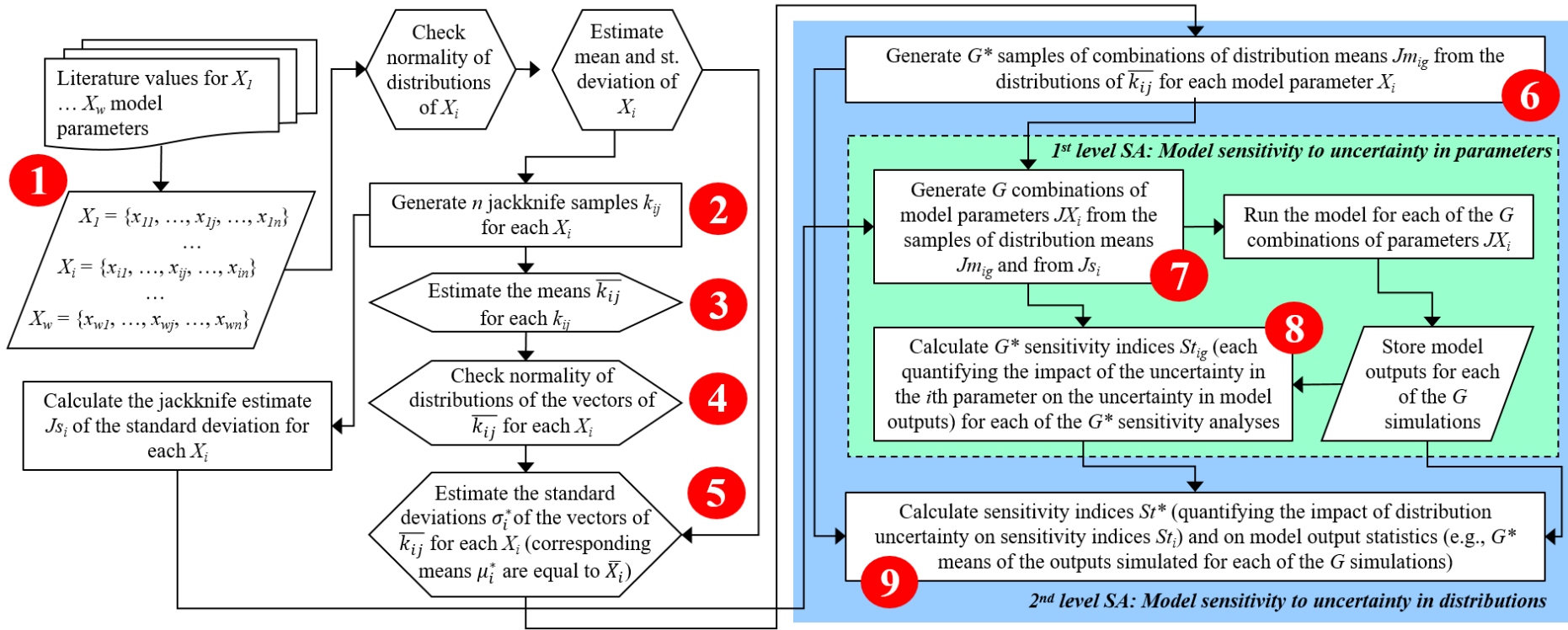


# Sensitivity analysis

Development of crop ideotypes

## Uncertainty in sensitivity analysis

- Most **methods** are very sensitive to **parameter distributions**







# Sensitivity analysis

Development of crop ideotypes

## Uncertainty in sensitivity analysis

- Most **methods** are very sensitive to **parameter distributions**

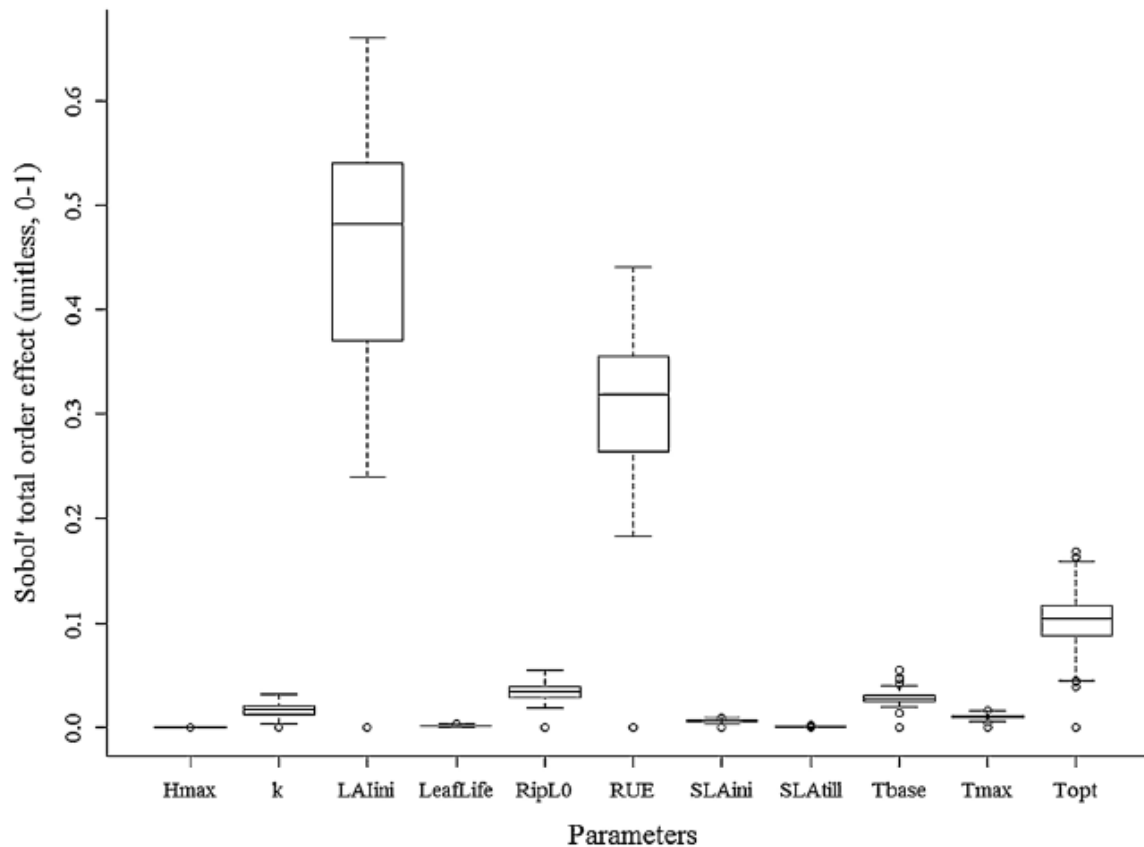


Fig. 2. Box plots of the Sobol' total order effects ( $St$ ) for model parameters obtained for the 6144 1st level sensitivity analyses. Variability results from the use of different distributions (generated) for model parameters.



# Sensitivity analysis

Development of crop ideotypes

## Uncertainty in sensitivity analysis

- **Sensitivity** analysis is **situational!**

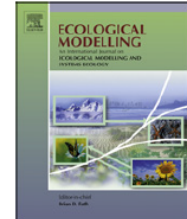
Ecological Modelling 225 (2012) 159–166



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Quantifying plasticity in simulation models

R. Confalonieri<sup>a,\*</sup>, S. Bregaglio<sup>a,b</sup>, M. Acutis<sup>a</sup>



# Sensitivity analysis

Development of crop ideotypes

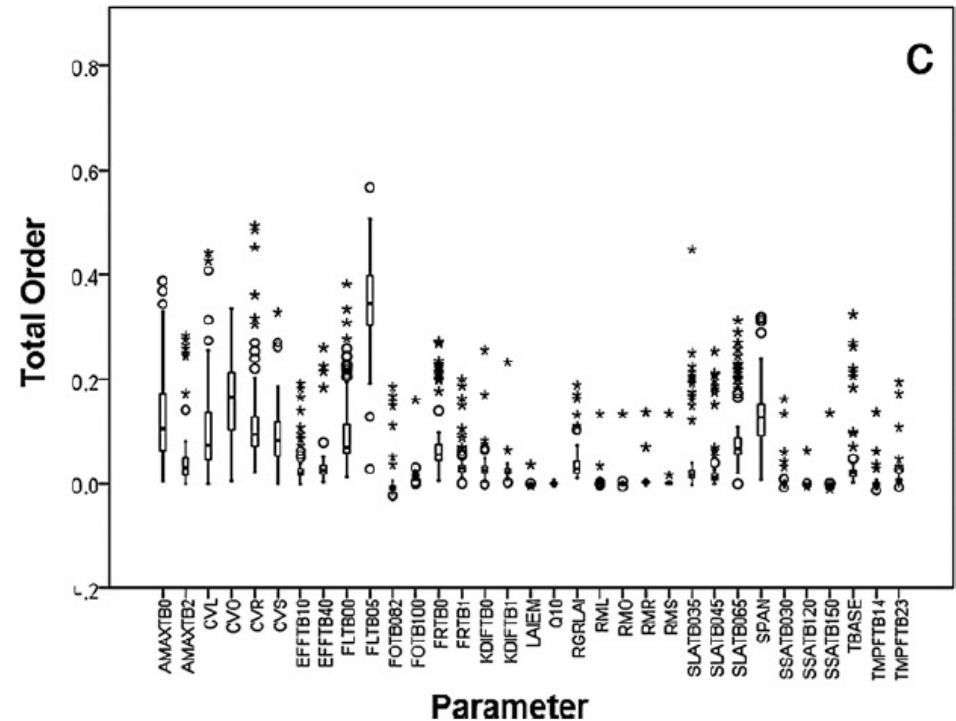
## Uncertainty in sensitivity analysis

- **Sensitivity** analysis is **situational!**
  - ✓ WOFOST model, rice
  - ✓ 10 locations, three diverging seasons per location
  - ✓ Output: aboveground biomass

- **Crucial for ideotyping**



- **District-specific ideotypes**





# In silico ideotyping

## Development of crop ideotypes

1. Define **ranges/statistical distributions** for **trait** values
2. Identify **most relevant traits**
  - ✓ Global **sensitivity analysis**
3. Define “**optimal**” **values** for those traits (targeting specific **objective functions**)
  - ✓ Trial and error/grid search

Europ. J. Agronomy 82 (2017) 144–162



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European Journal of Agronomy

journal homepage: [www.elsevier.com/locate/eja](http://www.elsevier.com/locate/eja)



## Designing future barley ideotypes using a crop model ensemble

Fulu Tao<sup>a,\*</sup>, Reimund P. Rötter<sup>a,b</sup>, Taru Palosuo<sup>a</sup>, C.G.H. Díaz-Ambrona<sup>c</sup>, M. Inés Mínguez<sup>c</sup>, Mikhail A. Semenov<sup>d</sup>, Kurt Christian Kersebaum<sup>e</sup>, Claas Nendel<sup>e</sup>, Davide Cammarano<sup>f</sup>, Holger Hoffmann<sup>g</sup>, Frank Ewert<sup>g</sup>, Anelle Dambreville<sup>h</sup>, Pierre Martre<sup>h</sup>, Lucía Rodríguez<sup>c</sup>, Margarita Ruiz-Ramos<sup>c</sup>, Thomas Gaiser<sup>g</sup>, Jukka G. Höhn<sup>a</sup>, Tapio Salo<sup>a</sup>, Roberto Ferrise<sup>i</sup>, Marco Bindi<sup>i</sup>, Alan H. Schulman<sup>a,j</sup>





# Trial and error

## Development of crop ideotypes

- Once most relevant parameters have been identified



- Calibration of model parameters



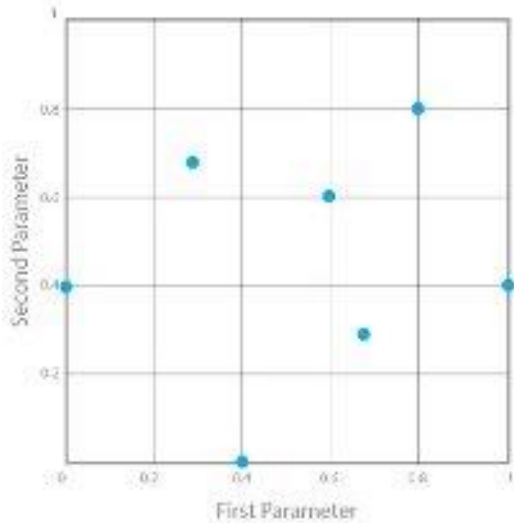
# Grid search

Development of crop ideotypes

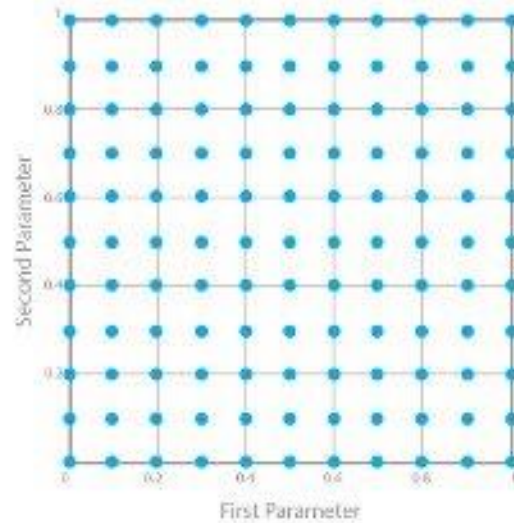
- Once most relevant parameters have been identified



Manual Search



Grid Search





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3. Define **“optimal” values** for those traits (targeting specific **objective functions**)
  - ✓ Trial and error/grid search
  - ✓ Automatic calibration algorithms

 Global Change Biology

celebrating 20 years

Global Change Biology (2014), doi: 10.1111/gcb.12567

## Simultaneous improvement in productivity, water use, and albedo through crop structural modification

DARREN T. DREWRY<sup>1,2</sup>, PRAVEEN KUMAR<sup>3,4</sup> and STEPHEN P. LONG<sup>5,6</sup>

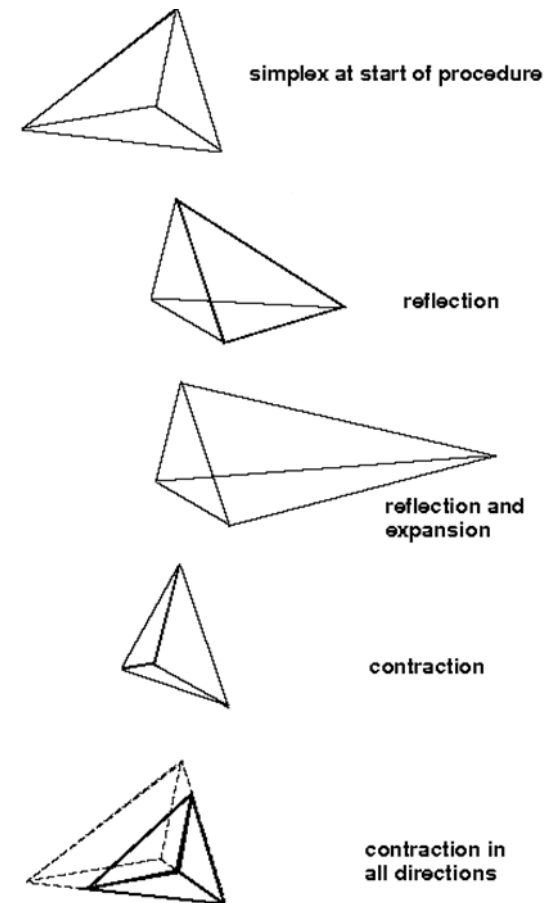
<sup>1</sup>Climate Physics Group, Jet Propulsion Laboratory, California Institute of Technology, m/s 233-300, Pasadena, CA 91109-8099, USA, <sup>2</sup>Joint Institute for Regional Earth System Science & Engineering, University of California Los Angeles, 607 Charles E Young Drive East, Young Hall, Room 4242, Los Angeles, CA 90095-7228, USA, <sup>3</sup>Department of Civil and Environmental Engineering, University of Illinois, 2527B Hydrosystems Laboratory, 301 North Mathews Avenue, Urbana, IL 61801-2352, USA, <sup>4</sup>Department of Atmospheric Sciences, University of Illinois, 150 South Gregory Street, Urbana, IL 61801-3070, USA, <sup>5</sup>Department of Crop Sciences, University of Illinois, AW-101 Turner Hall, 1102 South Goodwin Avenue, Urbana, IL 61801, USA, <sup>6</sup>Department of Plant Biology, University of Illinois, 265 Morrill Hall, 505 South Goodwin Avenue, Urbana, IL 61801, USA



# Optimization

## Development of crop ideotypes

- There are **different optimization algorithms**
  - ✓ The **downhill simplex** is often considered as one of those with the best “value for money”
  - ✓ Parameters with a biophysical meaning → use a **bounded simplex**
  - ✓ **Evolutionary shuffled simplex**, developed to reduce the risk to fall in local minima
  - ✓ **Easy** to implement
  - ✓ **Fast**



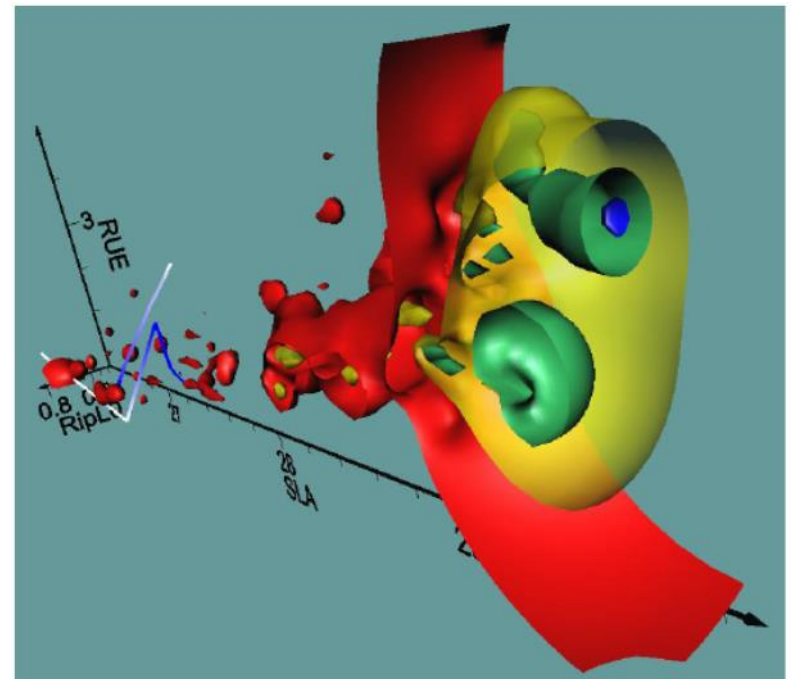




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## Development of crop ideotypes

1. Define **ranges/statistical distributions** for **trait** values

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✓ Trial and error/grid search

✓ Automatic calibration algorithms

✓ From sensitivity analysis results

Ecological Modelling 340 (2016) 57–63

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Sensitivity analysis of a sensitivity analysis: We are likely overlooking the impact of distributional assumptions

Livia Paleari<sup>a</sup>, Roberto Confalonieri<sup>b,\*</sup>

CrossMark



# Ideotype definition

## Development of crop ideotypes

- From sensitivity analysis results
  - ✓ Deriving putative ideotypes **considering both performance and extent of the improvement** required
  - ✓ **Avoiding local minima**

$$I_{\text{ideo}} = \left[ \sum_{i=1}^n \left( \left( \frac{|x_i - m_i|}{m_i} \cdot 100 \right) \cdot \frac{1}{\sqrt{St_i}} \right) \cdot \frac{1}{n} \right] \cdot \left( 1 - \frac{Y_v}{Y_{vmax}} \right)$$

- $n$ : number of parameters defining the ideotype;
- $x_i$ : value of the  $i$ th parameter
- $m_i$ : distribution mean of the  $i$ th parameter
- $St_i$ : Sobol' total order for the  $i$ th parameter
- $Y_v$ : **economical yield** from the ideotype (e.g., grain quality)
- $Y_v/Y_{vmax}$ : yield of the ideotype (€ ha<sup>-1</sup>) normalized to the maximum of all ideotypes under evaluation

- **Ideotype profile:**  
average values of the **best 1%**



# In silico ideotyping

## Development of crop ideotypes

- **Sample results**

- ✓ WARM rice model
- ✓ Traits involved with different processes
  - growth
  - sterility due to cold/heat shocks around flowering
  - plant-pathogen interactions
  - grain quality
- ✓ 5 sites



# In silico ideotyping

## Development of crop ideotypes

	Los Baños	Ludhiana	Nanjing	Shizukuishi	Milan
<b>Country</b>	<b>Philippines</b>	<b>India</b>	<b>China</b>	<b>Japan</b>	<b>Italy</b>
Coordinates	121°9'E, 14°6'N	75°48'E, 30°54'N	118°59'E, 32°56'N	140°57'E, 39°41'N	8°41'E, 45°4'N
Climate type	Tropical, humid	Subtropical, semiarid	Subtropical, semihumid	Cool temperate, humid	Temperate, semiarid
Mean T max (°C)	30.2	29.3	20.3	13.7	18.2
Mean T min (°C)	23.2	16.8	12.0	5.1	8.6
Mean rad (MJ m <sup>-2</sup> )	15.9	18.7	14.1	12.1	14.6
Rainfall (mm)	2060	703	1076	1557	698
Emberger continentality (Tmax warmest month – Tmin coldest month)	11.0 (oceanic insular)	31.8 (semi- continental)	32.3 (semi- continental)	33.1 (semi- continental)	31.1 (semi- continental)
SAM Aridity index (ET0-Rain)/(ED0+Rain)	0.13	-0.39	-0.20	-0.01	-0.36



# In silico ideotyping

## Development of crop ideotypes

- **Sample results**

- ✓ WARM rice model
- ✓ Traits involved with different processes
  - growth
  - sterility due to cold/heat shocks around flowering
  - plant-pathogen interactions
  - grain quality
- ✓ 5 sites
- ✓ Different climate scenarios
  - supporting the development of new varieties suitable in the mid-term



# In silico ideotyping

## Development of crop ideotypes

- **Climate scenarios**

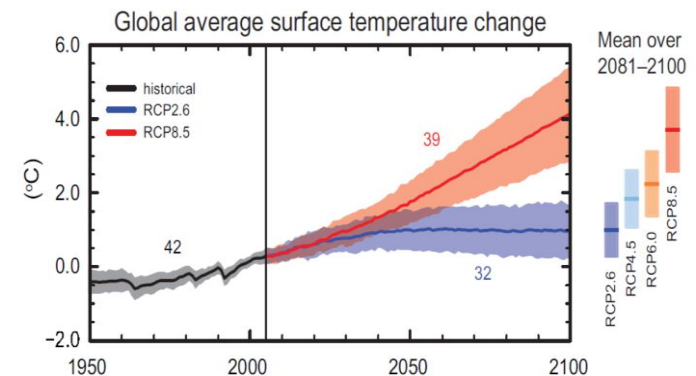
- ✓ **4 20-year time frames:** 1986-2005 (baseline), 2030, 2050, 2070
- ✓ **2 IPCC AR5:** RCP2.6, RCP8.5
- ✓ **2 GCMs:** HadGEM2, GISS-ModelE2
- ✓ **WG:** CLIMAK

- **Ideotyping**

- ✓ Sensitivity analysis method: Sobol' – total order effect

- **Variable analyzed:** Value  $\text{ha}^{-1} \rightarrow \text{YL} \cdot \text{V} - \text{YL} \cdot [(1-\text{HR}) + \text{C}] \cdot \text{V} / 2$

- ✓ YL ( $\text{t ha}^{-1}$ ): yield limited by biotic/abiotic factors
- ✓ V (euros  $\text{t}^{-1}$ ): value of entire and non chalky grains
- ✓ HR (-, 0-1): head rice yield
- ✓ C (-, 0-1): chalkiness



More than 6.6 million simulations